

Evidence for orbital Fulde-Ferrell-Larkin-Ovchinnikov state in the bulk limit of 2H-NbSe₂

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The Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) state is an unusual superconducting phase that survives beyond the Pauli paramagnetic limit through spatial modulation of the order parameter. An even more exotic variant—the orbital FFLO state—was recently reported in thin flakes of 2H-NbSe₂, involving the interplay of Ising spin-orbit coupling and orbital pair breaking. Here, we report thermodynamic signatures consistent with an orbital FFLO state in bulk 2H-NbSe₂, based on high-resolution magnetization and torque measurements under strictly parallel to the NbSe₂ basal plane. In the magnetic phase diagram, a crossover to a first-order transition appears above 3 T and disappears with slight field misalignment, indicating field-angle dependent Pauli-limited behavior. Additionally, we observe a reversible step-like anomaly within the superconducting state, and a pronounced six-fold in-plane modulation of the upper critical field above this phase transition. These results suggest that the orbital FFLO state is likely realized even in the bulk limit of 2H-NbSe₂.

Superconducting transition metal dichalcogenides (TMDs) with their strongly anisotropic layered structures exhibit remarkable resilience against strong magnetic fields, especially when these fields align parallel to their layered structure. This resilience manifests differently in two-dimensional (2D) and three-dimensional (3D) forms of TMDs. In the 2D form, the unique combination of an open Fermi surface and a specific type of Ising spin orbital coupling (SOC) neutralizes the conventional upper critical field mechanism^{1–3}. On the other hand, in the 3D form, the emergence of unconventional Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) phases under the influence of a magnetic field contributes to a similar effect^{4,5}.

When a spin-singlet type-II superconductor is exposed to a magnetic field, there are two distinct mechanisms which suppress superconductivity and restore the normal metallic state at the upper critical field H_{c2} . In most superconductors this is driven by the orbital effect, where the superconducting screening currents reach a pair breaking value, inducing a continuous second-order transition to the normal state⁶. An alternative mechanism is based on the Zeeman effect: when the Zeeman splitting energy between the two electrons of opposite spins, which form the Cooper pair, attains a value that abruptly breaks up all pairs. This occurs at the Pauli limiting field, which is theoretically the maximum magnetic field threshold for superconductivity. This Pauli limit results in a sudden, discontinuous first-order phase

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transition, restoring the normal state. However, this limit is seldom observed because most spin-singlet superconductors never attain this Pauli limit. In fact, H_{c2} for the majority of type-II superconductors typically occurs at much lower fields and is driven by the orbital effect. In the case of strongly anisotropic layered superconductors, an exception can occur when the magnetic field is applied strictly parallel to the layers^{4,7–21}. When the interlayer coupling is weak, the orbital effect is suppressed, allowing the orbital limit to surpass the Pauli limit^{22,23}. Typically, the H_{c2} transition line in the magnetic field versus temperature phase diagram then exhibits a steep initial slope, but it plateaus at the Pauli limiting field due to the abrupt suppression of superconductivity by the Zeeman effect.

The FFLO state^{24,25}, an unusual superconducting state, can manifest under specific conditions in type-II spin-singlet superconductors when they exceed the Pauli limit. The formation of the FFLO state provides a solution for the superconductor to preserve its superconducting state even above the Pauli limit. This is achieved by forming Cooper pairs with finite center-of-mass momentum. In this state, the amplitude of the superconducting order parameter undergoes spatial modulation, enabling the superconductor to exist in fields beyond the Pauli limit. To date, it has been observed in very few superconductors, which include organic superconductors^{10–20}, and the heavy-fermion superconductor CeCoIn₅, where the FFLO state coexists with a spin density wave^{7–9}. Other instances of this phenomenon have been reported in the iron-based superconductors FeSe²⁶ and KFe₂As₂²¹.

Some TMD materials are intrinsic superconductors, including 2H-NbSe₂ and 2H-NbS₂ with critical temperatures of 7.2 K and 5.5 K in their bulk form, respectively. TMD superconductors are in principle ideal materials for searching for FFLO states. Their layered structure causes high upper critical fields when the field is applied parallel to the layers, which can exceed (2H-NbS₂⁴) or come close to the Pauli limit (2H-NbSe₂²⁷). The FFLO state can be realized if the superconductor is in the clean limit with a long electron mean-free-path surpassing the coherence length²⁸, a condition which is met in TMD materials²⁹. Recent studies conducted by some of us, have reported thermodynamic evidence for the FFLO state in 2H-NbS₂⁴. The H_{c2} transition line of 2H-NbS₂ was found to surpass the Pauli limit at 10 T and exceeded 15 T. Furthermore, the characteristic upturn of the upper critical field line was observed above the Pauli limit, along with an additional field-induced phase transition line near the Pauli limit. These are indicative of the formation of an FFLO state, with the additional phase transition line representing the transition from the ordinary low-field superconducting phase to the high field FFLO phase. Notably, the additional phase transition line distinguishes the nature of the high field phase from Ising superconductivity, which has been found in TMD superconductors in the 2D limit to provide an alternative route to superconductivity beyond the Pauli limit due to a locking of the electron spins to the direction perpendicular to the basal plane^{1–3}.

The sister TMD compound, 2H-NbSe₂, contrasts in that it approaches, but does not exceed the Pauli limit due to its significantly weaker anisotropy²⁷. This results in a relatively strong orbital effect that prevents it from surpassing the Pauli limit, thereby excluding the formation of the regular FFLO state. However, a new type of so-called orbital FFLO state³⁰ has recently been reported for less than ~40 nm thick 2D 2H-NbSe₂ samples⁵. The interlayer orbital effect, caused by the external magnetic field, can facilitate FFLO formation in an Ising superconductor, where the Zeeman effect is essentially inhibited due to the strong Ising-type of spin-orbit coupling. This mechanism can establish the FFLO state at field strengths significantly below the Pauli limit. Transport measurements have indicated broken translational and rotational symmetries in the orbital FFLO state, which were interpreted as characteristic signs of finite-momentum Cooper pairings.

While these results provided the first experimental evidence for orbital FFLO pairing in the two-dimensional limit, they relied on

indirect signatures obtained from transport measurements and were limited to thin flakes from the 2D limit up to tens of nanometers. In contrast, the present study focuses on true bulk single crystals (~100 nm thick), where thermodynamic signatures of the FFLO phase can be directly resolved. Interestingly, we find that even in this bulk limit—where inversion symmetry is restored and Ising spin-orbit coupling is expected to be significantly reduced—consistent with an orbital FFLO phase.

In this article, we provide thermodynamic evidence for the potential existence of an orbital FFLO state in a micro-meter thick 3D bulk single crystalline sample of 2H-NbSe₂. We conducted high-resolution DC magnetization experiments in combination with electrical transport, and we reanalyzed magnetic torque data²⁷, all with a magnetic field orientation strictly parallel to the basal plane formed by the NbSe₂ layers. See refs. 4, 27 for a detailed description of the alignment procedure. As previously reported²⁷, the H_{c2} extrapolates to a magnetic field of 11.4 T at zero temperature when the field is aligned within 0.1 degree with respect to the parallel orientation. This is below the theoretical weak coupling Pauli limit, which can be estimated using the BCS approach as $H_p = 1.85T_c = 13.3$ T. However, when we apply magnetic fields of 3 T and above, the superconducting transition already exhibits weakly first-order behavior at the upper critical field line, which is absent for misalignments on the order of 1 degree. This phenomenon typically indicates that Pauli paramagnetic effects are beginning to exert a pair breaking influence. In addition, we report here a sharp step-like anomaly appearing in the reversible component of the magnetization and magnetic torque within the superconducting state. This forms a phase transition line with a slight downward trend upon increasing temperature, clearly indicating the thermodynamic signature of a phase transition separating the ordinary low-field superconducting phase from an unusual high magnetic field state. Furthermore, our precise field-angle resolved electrical transport experiments revealed that the critical field line develops a six-fold symmetry in the field range where this high-field phase occurs. These observations, which were considered to be the hallmarks of the orbital FFLO state in ref. 5, suggest the possible existence of an orbital FFLO state even in the three-dimensional bulk limit of 2H-NbSe₂ samples, making this novel pair density wave state highly accessible in very clean bulk samples and within a temperature and field range that can be accessed in a standard low-temperature laboratory.

Results

DC magnetization experiments

In Fig. 1 we present DC magnetization data obtained from a 2H-NbSe₂ single crystal²⁷. Data taken under zero-field-cooled (ZFC) and field-cooled (FC) conditions in a weak 5 Oe applied magnetic field show the zero-field superconducting transition to occur at 7.2 K (Fig. 1a). Measurements in higher magnetic fields up to 7 T were conducted as a function of temperature with a constant field applied parallel to the layered structure (Fig. 1b). At low magnetic fields up to 2 T, we identify a typical kink-like second-order phase transition occurring at the critical temperature. In higher fields (3 T–7 T) a small step-like feature emerges below the critical temperature (see arrow for the 7 T data), indicating a first-order phase transition. The temperature derivative of the magnetization $dM(T)/dT$ (main panel, Fig. 1c) reveals more about the phase transition behavior. In the range up to 2 T, the superconducting transition exhibits a step-like behavior, which is the expected behavior for a thermodynamic quantity being the second temperature derivative of the free energy (like the well-known superconducting specific heat transition at T_c). At a magnetic field strength of 3 T, a sharp peak emerges on top of the step-like transition anomaly. As the magnetic field increases further, this peak becomes dominant, which is a characteristic behavior of a first-order transition. The observed field-induced change in the order of the superconducting transition is usually only known to occur in Type-II superconductors

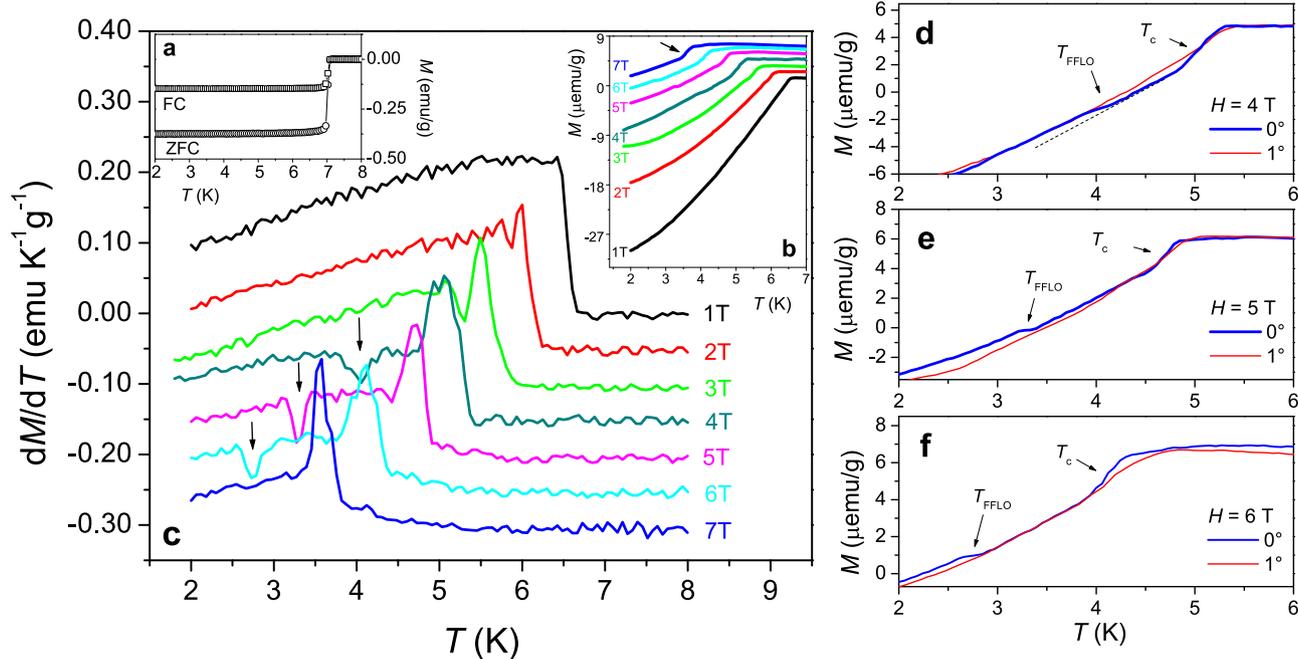


Fig. 1 | DC magnetization data of 2H-NbSe₂ in magnetic fields applied parallel to the basal plane. **a** Low field data measured in a 5 Oe applied magnetic field under zero-field-cooled (ZFC) and field-cooled (FC) conditions. It shows the superconducting transition at $T_c = 7.2$ K. **b** High-field data from 1 – 7 T. The ZFC and FC data was almost identical and only ZFC data is shown. Offsets of 0.025 $\mu\text{emu}\cdot\text{g}^{-1}$ have been added for clarity, except for the 1 T-data. Main panel **c**, temperature derivative of the high field data $dM(T)/dT$, showing the development of a first-order transition peak-like anomaly at the superconducting transition in fields above 3 T and small

dips at the FFLO transition in 3, 4 and 5 T as marked by the arrows. Negative offsets of 0.05 $\mu\text{emu}\cdot\text{K}^{-1}\cdot\text{g}^{-1}$ have been added for clarity, except for the 1T-data. **d–f** Details of the original magnetization data in 4, 5 and 6 T in fields applied strictly parallel to the basal plane (0°) and for a small misalignment (-1°). Step like anomalies appear at the FFLO transition and at T_c only for the 0° data, while for a small misalignment the transition at T_c adopts a more continuous kink-like nature without any FFLO transition.

due to the Pauli paramagnetic effect and may indicate that this effect is present here at surprisingly low magnetic fields, given that the theoretical Pauli limit for 2H-NbSe₂ with a 7.2 K- T_c is roughly estimated to occur near 13 T. A further peculiarity are dip-like transition anomalies occurring in the field range from 4 T to 6 T in $dM(T)/dT$, which are also visible in form of an additional tiny step-like transition in the magnetization $M(T)$ as shown in the enlarged data in panels d – f. These steps disappear completely when introducing a small field/basal plane misalignment on the order of 1 degree. We will later identify them as a transition into an orbital FFLO state occurring at characteristic temperatures T_{FFLO} .

Although the step-like anomaly in the magnetization may appear tiny, it is observed consistently across different samples, appears only under precise field alignment, and exhibits a reversible and well-defined temperature dependence. These features strongly suggest that the anomaly originates from a generic bulk thermodynamic transition rather than a surface-related effect. Additionally, we do not observe similar anomalies for perpendicular fields²⁷, which further rules out surface superconductivity as the likely cause. Further details and analysis will be provided later in our discussion.

Magnetic torque experiments

Figure 2a shows the magnetic torque at $T = 0.3$ K as a function of the magnetic field applied strictly parallel to the basal plane. Coming from zero field, the torque signal increases rapidly at small fields towards positive values (see arrow for field sweep direction), reaches a maximum, and then initially decreases. Above 7 T, the torque begins to rise again at higher fields, forming a pronounced peak effect anomaly due to enhanced flux pinning³¹, before abruptly dropping to a small background value in the normal state at H_{c2} . Such a sharp decay of the screening currents is usually observed in Pauli-limited superconductors and associated with a first-order nature of the H_{c2}

transition triggered by the Pauli paramagnetic effect^{4,12,21}, thus confirming the findings from the DC magnetization data. Upon decreasing the field, the torque changes sign and the H_{c2} transition appears more continuous, indicating the gradual building up of screening currents in the opposite direction when the field is lowered below H_{c2} .

Figure 2b shows details of the magnetic torque in the upward sweep data, where small jump-like anomalies appear below the onset of the peak-like anomalies for all temperatures up to 2.4 K (see arrow with label H_{FFLO} marked for the example of the 0.3 K data). We will attribute these in the following to the transition between the ordinary low field superconducting state and the orbital FFLO state in higher fields. In Fig. 2a, we also mark a small change of slope in the 0.3 K data in the downward sweep near 9 T, which we will demonstrate in the following is due to the same phase transition at H_{FFLO} .

The inset of Fig. 2b shows temperature dependent magnetic torque data in a 7.5 T magnetic field, which also shows a broad small step-like anomaly, suggesting that this measurement crosses the FFLO transition line as a function of temperature.

Figure 2c shows magnetic torque data near the anomalies at H_{FFLO} for increasing field for the layered organic FFLO superconductor κ -(BEDT-TTF)₂Cu(NCS)₂ for comparison¹². Both superconductors feature small step-like anomalies at H_{FFLO} which look very similar, suggesting that they may have the same origin. The step occurs in both compounds slightly below a pronounced peak in the torque just before the rapid drop of the signal occurs when approaching the upper critical field. Numerous reports have confirmed the presence of an FFLO state in parallel fields above the Pauli limit at 21 T^{11,12,15–18}, which occurs in that compound near the Pauli limit of 21 T as shown here by the small step-like anomaly. It is evident that the transition between the ordinary superconducting state at low-fields and the FFLO state at high fields above -21 T presents a very similar response of the magnetic torque in the form of a small, slightly broadened downward step, as

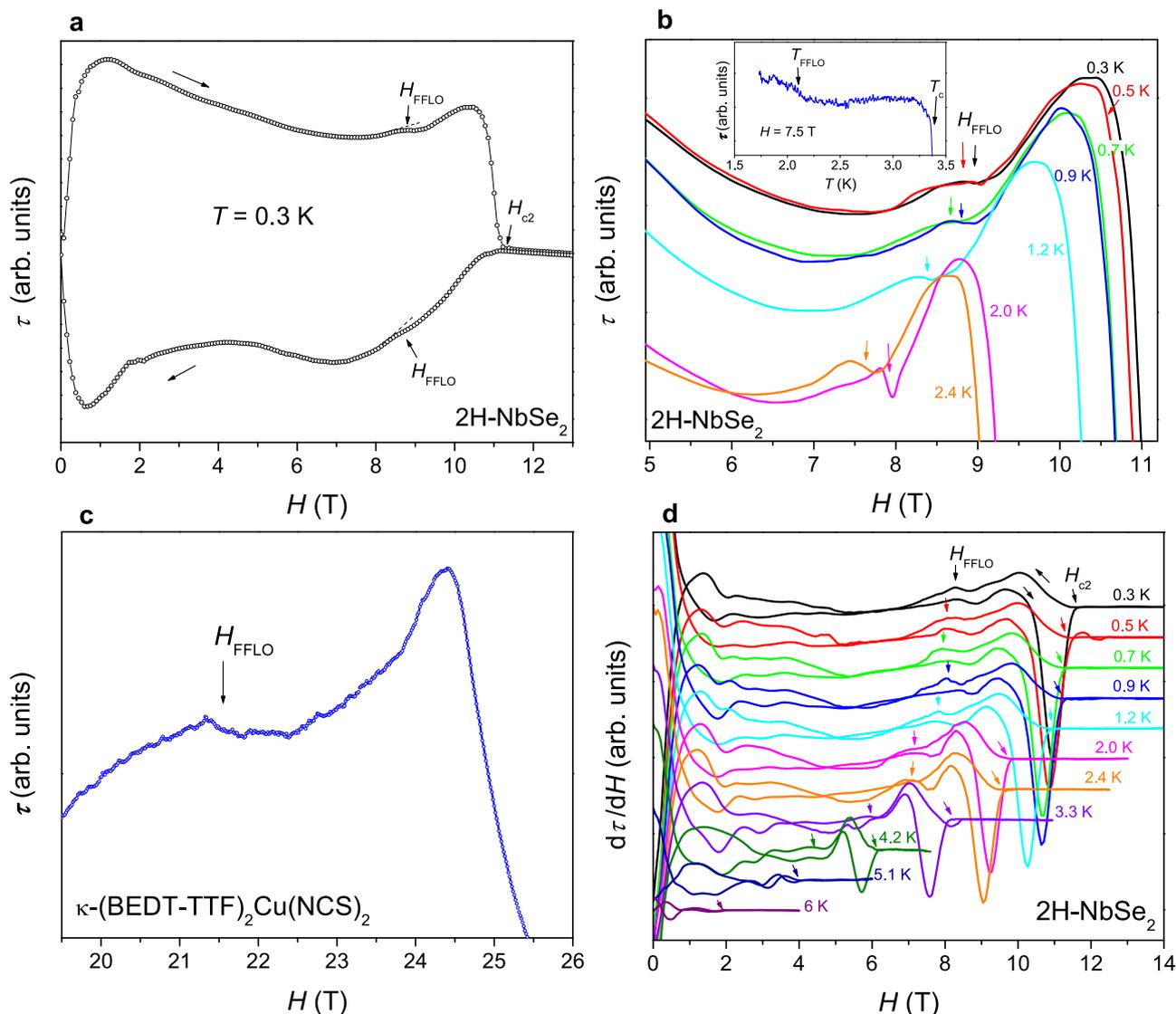


Fig. 2 | Magnetic torque data in magnetic fields applied parallel to the basal plane. **a** Magnetic torque magnitude $\tau(H)$ measured at $T = 0.3$ K as a function of increasing and decreasing magnetic field (see arrows). H_{c2} is marked by an arrow. The additional arrow indicates the position of an additional small phase transition anomaly attributed to the transition into the orbital FFLO state (H_{FFLO}). **b** Magnetic torque data $\tau(H)$ of 2H-NbSe₂ measured at various fixed temperatures as a function of increasing parallel magnetic field offering an enlarged view on the small step-like anomalies at H_{FFLO} . Inset: Temperature dependent measurement of the magnetic torque magnitude $\tau(T)$ in a 7.5 T parallel magnetic field, which crosses the FFLO

transition line at T_{FFLO} . **c** Similar enlarged view on the magnetic torque magnitude $\tau(H)$ of the layered organic FFLO superconductor κ -(BEDT-TTF)₂Cu(NCS)₂ as in **(a, b)** measured at a fixed temperature of $T = 1.7$ K as a function of increasing magnetic field applied parallel to the layered structure showing a very similar small step-like anomalies at H_{FFLO} . **d** Magnetic field derivative of the magnetic torque magnitude $d\tau(H)/dH$ showing the transition anomalies at H_{FFLO} in both the ascending and descending branches clearer. Arrows mark the transitions at H_{c2} and H_{FFLO} . Offsets have been added for clarity.

marked by the arrows in Fig. 2a, b. For 2H-NbSe₂, the Pauli paramagnetic effect may already be strong enough to trigger an FFLO state and thus produce such a reversible anomaly in the torque.

Figure 2d shows the first field derivative of the magnetic torque, calculated from the smoothed data in Fig. 2a, b, which shows the anomalies at H_{FFLO} as small bumps as marked by the vertical arrows. They can be traced up to 2.4 K. Note that the anomaly in the original torque data for decreasing fields is partially hidden by the slope of the broad upper critical field transition, but it is evident here in the field derivative, in which the background slope is transformed into an almost constant contribution.

Magnetic phase diagram

In Fig. 3, we plot the extracted $H_{c2}(T)$, $H_{\text{FFLO}}(T)$, $T_c(H)$ and $T_{\text{FFLO}}(H)$ values of 2H-NbSe₂ for the parallel field direction with respect to the

basal plane of the layered structure in a magnetic phase diagram. H_{c2} was taken as the upper limit at which the torque deviates from the small normal state background. Although H_{c2} in 2H-NbSe₂ does not reach the theoretical Pauli limit, all torque data measured up to 4.2 K show the small reversible torque anomaly, indicating a phase transition within the superconducting state, which is also visible in the temperature dependent measurement of the DC magnetization. While the strong orbital effects naively suggest that no FFLO state should form, even though the paramagnetic effect could have an impact as early as 3 T (suggested by peak-like anomalies in the temperature derivative of the DC magnetization in Fig. 1 and the rapid decay of screening currents in the torque below H_{c2}), it is interesting that this line appears in the phase diagram of 2H-NbSe₂. Indeed, such a transition line would be expected during the formation of the FFLO state^{4,8,12,21}. We will later discuss that this agrees indeed with the

theoretical expectation for the new type of orbital FFLO state observed here in the thick bulk limit of 2H-NbSe₂.

Another peculiarity is that the upper critical field line deviates near 3 T from the Werthamer–Helfand–Hohenberg (WHH) model

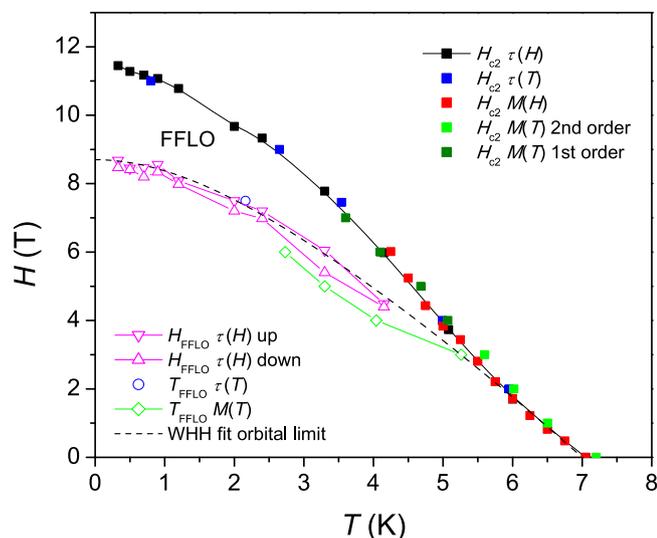


Fig. 3 | Magnetic phase diagram of 2H-NbSe₂ in magnetic fields applied strictly parallel to the layer structure. The data were obtained from magnetic torque measurements and below 7 T by DC magnetization measurements conducted as a function of field $M(H)$ or temperature $M(T)$ ²⁷. The continuous black line marks the H_{c2} line as obtained from the various datasets. Black squares represent H_{c2} data as obtained from the data shown in Fig. 2 $\tau(H)$. Blue squares have been obtained from temperature dependent magnetic torque measurements $\tau(T)$ ²⁷. The magenta-colored triangles mark the small additional reversible anomalies in $\tau(H)$ attributed to a phase transition between the ordinary superconducting state at low fields and the high-field orbital FFLO phase (H_{FFLO}), where upright, $\tau(H)$ up, (downright, $\tau(H)$ down) triangles have been measured upon increasing (decreasing) field. The blue circle marks a small downward step-like anomaly in a temperature dependent torque measurement which crosses the FFLO transition line at T_{FFLO} ²⁷. Green data is obtained from DC magnetization (light green squares: second-order transition at T_c , dark green first-order transition). The open diamonds mark the FFLO transition from the $M(T)$ data. We also used a fit of the standard Werthamer–Helfand–Hohenberg (WHH) model (dashed line) for the orbital limit of superconductivity fitted to the data below 2 T, which surprisingly stays below the H_{c2} line in higher fields, but perfectly follows the line of the FFLO transition.

which represents the orbital limit, which we fit to the data in the low field range below 2 T in form of an upturn at around 3 T, which is also the field where the FFLO transition line appears to meet the H_{c2} line in form of a tri-critical point. This could indeed represent the characteristic upturn of the H_{c2} line when the orbital FFLO state forms, which stabilizes superconductivity above the orbital limit.

Field-angle-resolved resistivity experiments

In Fig. 4 we present polar plots of the critical temperature T_c measured in a 10 T (a) and 5 T (b) magnetic field as a function of the angular direction of the magnetic field within the basal plane of 2H-NbSe₂. Note that T_c measured in an applied field is directly related to H_{c2} and the data thus represents the in-plane anisotropy of the upper critical field transition line, which has been demonstrated to reflect the symmetry of the superconducting order parameter^{32,33}. The data has been obtained from electrical resistance measurements for many different orientations of the applied magnetic field, but all parallel to the basal plane. Figure 4c shows resistance data in zero field and at two selected angles of 0° and 30° in 5 T and 10 T magnetic field. We used the temperature at which the resistance reaches 90 % of the normal state resistance as criterion to determine $T_c(H)$, but very similar results are found for other criteria. Figure 4a displays a pronounced six-fold symmetry, with maxima approximately each 60 degrees, but with a slight two-fold distortion along the 120 degrees direction. In 5 T the six-fold symmetry is much less evident and almost vanishes. Note that both polar plots are plotted over the same temperature range of 0.4 K, which allows fair comparison of both datasets. The appearance of such a six-fold symmetry has been linked to the orbital FFLO state in 2D 2H-NbSe₂⁵, and our data suggests that it is caused by the unusual superconducting phase above H_{FFLO} .

Discussion

Our data reveals a phase transition line separating the superconducting phase in the magnetic field vs. temperature phase diagram of 2H-NbSe₂ into a low field region and a high field region which occurs at low temperatures near 8 T and descends towards higher temperatures down to at least 4 T. The observed field range aligns with the magnetic field interval where first-order transition anomalies manifest during the superconducting (upper critical field) transition in both DC magnetization and magnetic torque. This correspondence suggests the influence of Pauli paramagnetic pair breaking. Furthermore, a development of a two-fold distorted six-fold in-plane symmetry of the

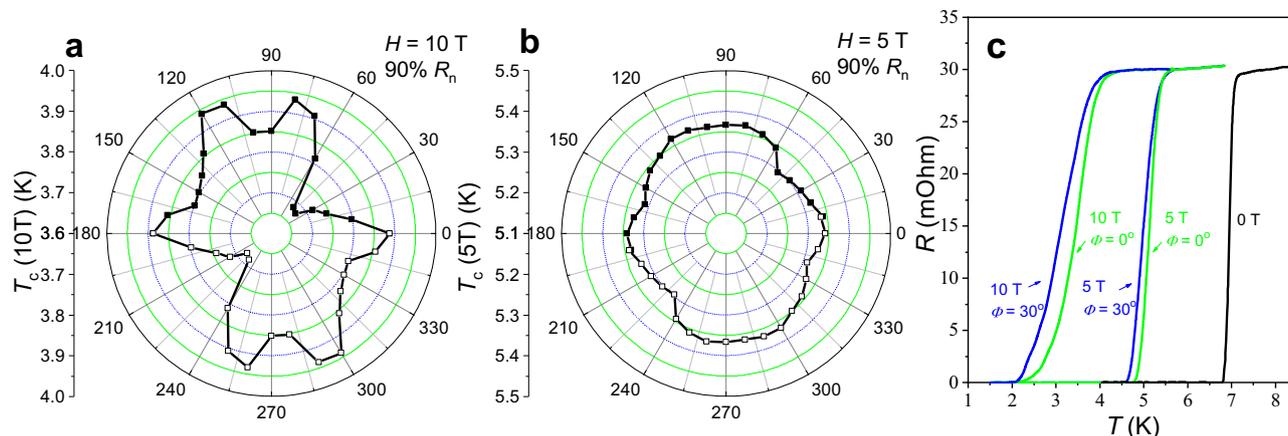


Fig. 4 | In-plane six-fold modulation of critical temperature. a, b Dependence of the critical temperature on the in-plane orientation of a magnetic field of 10 T and 5 T applied strictly parallel to the basal plane of 2H-NbSe₂. A slightly two-fold distorted six-fold symmetry is seen at 10 T. At 5 T the data is more isotropic. The critical temperature was defined when the resistance reaches 90 % of the normal

state resistance and the six-fold symmetry is much less evident. c Selected data of the electrical resistance in 0 T and for two different (5 T and 10 T) in-plane magnetic field orientations where a maximum ($\phi = 0^\circ$) and minimum ($\phi = 30^\circ$) critical temperature occur.

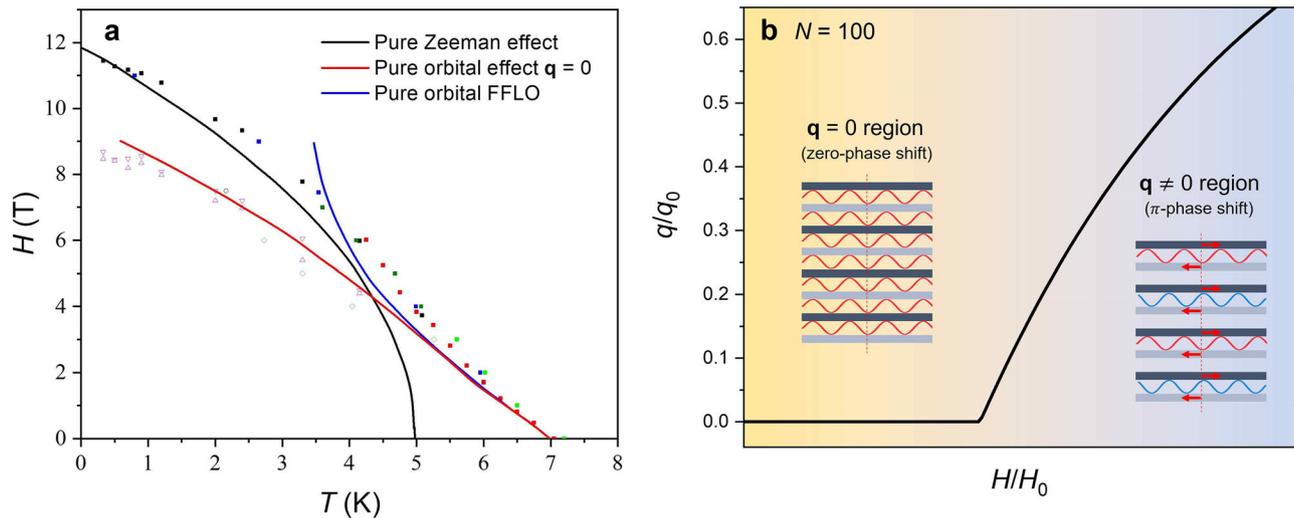


Fig. 5 | Theoretical interpretation and comparison with experiment for the orbital FFLO state. a Qualitative illustration of the temperature dependence of critical fields according to theoretical considerations (see ref. 35 for details). The blue and red lines represent the pure orbital effect, with finite Cooper pair momentum \mathbf{q} (blue) or $\mathbf{q} = 0$ (red), expected to be dominant in the high-temperature / low-field limit. The black line represents the low-temperature, high-field limit where the Zeeman effect decouples neighboring layers, making the depairing effect primarily due to the Zeeman effect within individual layers. This

line starts from the zero-field critical temperature of a monolayer. The symbols are experimental data identical to those shown in Fig. 3. **b** Field-induced evolution of the center-of-momentum \mathbf{q} in the orbital FFLO state. Calculated behavior of \mathbf{q}/q_0 as a function of in-plane magnetic field H/H_0 with $N = 100$ layers, based on ref. 35. At low fields, the superconducting state remains uniform with $\mathbf{q} = 0$, and the order parameter phase is aligned across layers (left schematic). At high fields, the inter-layer Josephson coupling is weakened, and a finite-momentum superconducting state emerges with alternating phase shifts, as shown in the right schematic.

upper critical field is observed, which has been reported to be a hallmark of the orbital FFLO phase in very thin flakes of NbSe₂ in the 2D limit⁵.

The phase transition anomaly occurs in the reversible component of the magnetic torque and is visible both in increasing and decreasing fields with only a marginal hysteresis, as well as in the temperature dependent DC magnetization measurement. Torque is directly related to the anisotropic component of magnetization, therefore the reversibility of this anomaly hints at a true thermodynamic phase transition as confirmed by its observation in the DC magnetization. This small phase transition at H_{FFLO} as well as the broad peak-like anomaly in the torque between H_{FFLO} and H_{c2} resemble clearly torque data of the layered organic superconductor κ -(BEDT-TTF)₂Cu(NCS)₂¹², where the small step-like anomaly and the peak have been shown to originate from the formation of an FFLO state above the Pauli limit. H_{c2} of 2H-NbSe₂ remains below the expected Pauli limit, even though it comes near to it, where Pauli paramagnetic effects may already play a role, as evidenced by the magnetization data. The broad pronounced peak effect below H_{c2} further indicates a change in the flux pinning properties between H_{FFLO} and H_{c2} , which can be plausibly explained by the formation of a spatially-modulation of the superconducting order parameter. Most importantly, the slope of the upper critical field line begins to deviate from the WHH model of the orbital limit of superconductivity, with an upward trend, in the field region where the FFLO transition line appears to meet the upper critical field line, likely representing the characteristic upturn of the upper critical field line that is considered a hallmark of the FFLO state.

Following the observation of a new type of orbital FFLO state^{30,34} in less than 40 nm thin 2H-NbSe₂ samples in ref. 5 a plausible explanation of our data is thus that this orbital FFLO state exists even in thick bulk samples. Supplementary Fig. S1 compares our bulk phase diagram with the case of 12 nm and 39 nm thin samples to illustrate the similarities. The observation of a thermodynamic phase transition line demonstrates the existence of an unusual magnetic field induced superconducting state. The uniqueness of this phase is its traceability to magnetic fields as low as 4 T and temperatures up to 4 K. The phase transition suggests that the tri-critical point where it intersects with the

superconducting transition line could be close to 5 K and fields between 3 T and 4 T. Here the H_{c2} transition line indeed shows an upturn and deviates from the WHH model as shown in Fig. 3⁵.

In the bilayer limit, orbital FFLO states can form under sufficiently high in-plane magnetic fields, with Cooper pairs on the two layers creating a Josephson vortex to screen the field³⁴. As the sample thickness increases, the number of Josephson vortices along the out-of-plane direction may also increase. When the thickness is smaller than the Josephson vortex size, only a single Josephson vortex will form, as observed in ref. 5. For larger thicknesses, multiple Josephson vortices can form, with their inter-vortex distance depending on the field strength. In the bulk limit, Josephson vortices can be closely packed along the out-of-plane direction, resulting in orbital FFLO states throughout the sample^{5,34}. At lower temperatures and higher fields, individual monolayers become decoupled because the Cooper pair momenta of adjacent monolayers are opposite. Consequently, the in-plane upper critical fields can be described by the monolayer limit as the temperature approaches zero.

In Fig. 5a, we qualitatively illustrate the three different limits affecting the phase transition lines in the magnetic phase diagram. The blue line and the red dashed line represent the pure orbital effect, with finite Cooper pair momentum \mathbf{q} (blue) or $\mathbf{q} = 0$ (red). These limits may apply to high temperatures and low fields, where Josephson couplings between different layers are significant. As the temperature decreases and the field increases, the Zeeman effect becomes prominent. In this scenario, neighboring layers have opposite Cooper pair momentum and weakly couple to each other. The depairing effect of the field is primarily due to the Zeeman effect within individual layers. This corresponds to the black line, which starts from the zero-field critical temperature of a monolayer, a value smaller than that of the bulk. The interplay of these temperature-dependent critical fields, driven by a dimensional crossover, can qualitatively explain the experimentally observed features in the phase diagram, including the formation of an orbital FFLO state.

To further elucidate how the orbital FFLO state evolves from the bilayer limit to the bulk, we reveal Fig. 5b, which schematically depicts the phase modulation across layers under increasing in-plane

magnetic field. In the low-field regime, the interlayer Josephson coupling enforces a uniform superconducting phase (i.e. $\mathbf{q} = 0$). As the field increases, the coupling weakens and finite-momentum pairing sets in, leading to alternating phase differences between neighboring layers (i.e. $\pm \mathbf{q}$). This modulation does not imply alternating magnetic flux, but instead reflects a spatially coherent phase arrangement of the superconducting order parameter. This picture supports the purely orbital origin of the FFLO phase, as predicted in ref. 35, and distinguishes it from surface Rashba-type helical states. Details about the Cooper pairing for the pure FFLO state and spin-orbit coupling assisted FFLO mechanisms are illustrated in Supplementary Fig. S2.

In ref. 27, it was shown that NbSe₂ is much less 2D than for example the FFLO superconductor NbS₂²⁷ with a much weaker anisotropy $\xi_{0\parallel}/\xi_{0\perp} = 2.29$ in contrast to $\xi_{0\parallel}/\xi_{0\perp} = 15$ in NbS₂. The orbital effect in NbSe₂ is thus quite strong, even in parallel magnetic fields, which has been attributed to the ratio of $\xi_{0\parallel}$ to the interlayer spacing d . The c -axis lattice parameter in the out-of-plane direction is about $d = 18 \text{ \AA}$ and the coherence length of NbSe₂ $\xi_{0\perp} = 31 \text{ \AA}$ is coupling adjacent layers strongly with strong Meissner currents in the out-of-plane direction, suppressing superconductivity by the orbital effect before the Pauli limit is reached. Nevertheless, it is likely that Ising spin orbit interaction still plays a role in bulk 2H-NbSe₂. Since it has been shown that the interlayer orbital effect, caused by the external magnetic field, can facilitate FFLO formation in an Ising superconductor, the FFLO state can indeed be established at field strengths significantly below the Pauli limit⁵. After all, even 30 nm for which the orbital FFLO state has still been observed from upper critical field measurements, is already pretty much in the bulk limit with a large number of layers N . Thus, our observed phase transition possibly has the same physical origin as the one described in ref. 5.

An alternative interpretation could be a vortex melting transition, a phenomenon well-documented in the high-temperature cuprate superconductor YBa₂Cu₃O_{7- δ} ³⁵, which has also been considered for 2H-NbSe₂³⁶⁻³⁹. While this explanation is plausible for magnetic fields applied perpendicular to the layers, where an order-disorder transition has been directly observed using scanning tunneling microscopy³⁷, it becomes less likely for magnetic field orientations parallel to a strongly layered superconductor. In this case, the vortices exist as Josephson vortices situated between the layers, and the strong pinning effect of the layers would likely inhibit a vortex melting transition or at least push it very close to the upper critical field line. Crucially, our electrical resistance measurements demonstrate that even at magnetic fields as high as 10 T, where only the high-field phase is present, the resistance drops to zero. This unequivocally rules out the possibility of a vortex liquid state, which invariably exhibits a finite electrical resistance. Previous reports of a vortex melting transition for this parallel field orientation³⁹ could be alternatively explained by the orbital FFLO transition. The formation of an FFLO state, with its spatial modulation of the order parameter, could induce a similar change in the vortex response.

It is noteworthy that the upper critical field line of the sister compound NbS₂ is also significantly influenced by the orbital effect⁴. Consequently, the FFLO state in NbS₂ is also likely to be an orbital FFLO state, although it appears above the Pauli limit, unlike in NbSe₂. Additionally, ref. 12 demonstrated that for the organic superconductor κ -(BEDT-TTF)₂Cu(NCS)₂, the orbital effect can be induced by slightly tilting the magnetic field out of the parallel in-plane direction while maintaining the FFLO state. This indicates that the orbital FFLO state is not exclusive to thin NbSe₂ in the 2D limit and was recognized prior to its novelty claim in ref. 30.

Although a six-fold in-plane modulation of H_{c2} is observed in both monolayer and bulk 2H-NbSe₂, the underlying mechanisms are fundamentally distinct (Supplementary Table S1). In monolayers, the emergence of six-fold feature arises from the interplay between strong Ising SOC and the in-plane Zeeman effect in the presence of reduced C_{3v}

symmetry due to the substrate. Theoretical studies show that under these conditions, the superconducting gap closes along specific directions (Γ - M) as the Zeeman field exceeds the pairing strength, leading to the formation of six nodal points in momentum space^{5,40}. This nodal structure appears even at low fields across the superconducting phase⁴⁰. In contrast, our bulk data show that the six-fold modulation emerges only above a threshold field H_{FFLO} , concomitant with the onset of the orbital FFLO phase. This suggests that the anisotropy is not symmetry-inherited, but rather a field-induced signature of finite-momentum pairing enabled by interlayer orbital coupling and remain Ising SOC. Theoretical calculations³⁴ support this crossover from a uniform ($\mathbf{q} = 0$) to a modulated ($\mathbf{q} \neq 0$) phase as layers decouple at high fields. Importantly, the inversion symmetry of the bulk D_{6h} structure forbids linear-in-momentum SOCs, such as Rashba-type terms. This symmetry constraint implies that the observed six-fold modulation in H_{c2} cannot be attributed to intrinsic band structure effects. Instead, it is consistent with a field-induced orbital pairing mechanism that becomes active only above H_{FFLO} , where interlayer coupling is suppressed and finite-momentum superconductivity emerges.

We also rule out surface-related explanations. Surface superconductivity (e.g. H_{c3} effect) cannot account for the sharp thermodynamic anomalies observed well below H_{c2} in the present results, nor does it explain their sensitivity to angular alignment. Likewise, Rashba-type surface states are confined to topmost layers and cannot produce that the six-fold anisotropy and associated anomalies arise from a bulk orbital FFLO phase, not surface effects. In addition, our upper critical field line agrees perfectly with previous specific heat experiments which are not sensitive to surface superconductivity²⁹. Although similar angular modulations in H_{c2} have been reported in thin films with interface-induced Rashba SOC⁴¹, such mechanisms are unlikely here, as the observed anisotropy emerges only above H_{FFLO} , in a field-induced regime consistent with an interlayer orbital pairing scenario.

In conclusion, our experimental observations, when coupled with theoretical considerations³⁴, suggest that the formation of an orbital FFLO state provides a plausible explanation for the observed magnetic field vs. temperature phase diagram of bulk 2H-NbSe₂ in strictly parallel magnetic fields. This includes an additional phase transition line within the superconducting phase and a weakly first-order nature of the upper critical field transition line. This underscores the necessity for a thermodynamic probe to investigate the FFLO transition within the superconducting phase in thicker 2H-NbSe₂ samples. This is particularly important as the characteristic upturn of the H_{c2} line appears to become almost hidden when approaching the bulk limit.

Our results provide thermodynamic indications consistent with an orbital FFLO phase. However, final confirmation requires a microscopic method capable of resolving the spatial modulation of the superconducting order parameter. Techniques such as scanning tunneling microscopy (STM) or nuclear magnetic resonance (NMR) will be essential to directly verify the microscopic nature of this state.

Methods

Sample preparation

For this study, we employed two distinct high-quality 2H-NbSe₂ single crystals sourced independently. Remarkably, both crystals exhibited nearly identical superconducting parameters, with a critical temperature of 7.2 K and upper critical field lines in agreement. Sample 1 was used for all magnetic torque measurements, field-dependent DC magnetization measurements and electrical resistivity measurements, while Sample 2 was used for repeated DC magnetization measurements at fixed temperatures. Sample 1 was grown at Uppsala University using an evaporation technique detailed in previous literature^{4,42}. The specimen under study was measuring about 1 mm × 1 mm × 0.1 mm with surfaces that were optically flat. Sample 2 was measuring about 0.4 mm × 0.7 mm × 0.1 mm. It was grown at DGIST using the Se self-flux method. Nb slugs (99.95%, Alfa Aesar, USA) and Se shots (99.999%, Alfa

Aesar, USA) were mixed in a molar ratio of 4:96 and loaded into an alumina crucible, which was sealed in a thick quartz ampoule under vacuum. The mixture was heated to 1173 K for 9 h, maintained at this temperature for 24 h for complete melting, then cooled to 1123 K for 3 h, followed by a 10 h hold. The ampoule was gradually cooled to 1053 K at a rate of 1 K/h and centrifuged, resulting in 2H-NbSe₂ single crystals with hexagonal plate morphology.

Magnetization measurements

DC magnetization measurements were conducted at fixed temperatures during field sweeps through the entire hysteresis cycle and under zero-field cooled (ZFC) and field cooled (FC) conditions with a Quantum Design MPMS 3 VSM SQUID magnetometer in parallel magnetic fields up to 7 T. Since there was no apparent difference in the ZFC and FC data in magnetic field of 1 T or above, only ZFC data is shown for high fields.

Magnetic torque measurements

The magnetic torque, a vector quantity, is directly associated with the anisotropic component of the DC magnetization \mathbf{M} and is given by the equation $\boldsymbol{\tau} = \mathbf{M} \times \mathbf{B}$, where \mathbf{B} represents the applied magnetic field vector. This was measured employing a capacitive cantilever method^{4,12,21}. The sensor was installed on a piezo rotator in a 15 T magnet cryostat's ³He probe, enabling millidegree precision alignment of the sample's basal plane relative to the magnetic field was achieved by carefully rotating the sample until the torque signal was minimized under fixed magnetic field and temperature conditions^{4,12,21,27}. Field or temperature sweeps were conducted at rates of 0.1 - 0.5 T/min and 0.04 K/min, respectively. The 2H-NbSe₂ data shown here is identical to data included in ref. 27, but the publication of ref. 5 has stimulated us to reinvestigate our data with respect to a possible realization of the orbital FFLO state. The -100 microns thick sample was attached with highly diluted GE7031 varnish to the flat, polished cantilever plate of a capacitive torque sensor. Capacitance was measured using a General Radio 1615-A capacitance bridge combined with a SR830 digital lock-in amplifier. It should be noted that even at parallel field alignment with respect the basal plane of a superconductor the magnetic torque usually remains finite due to quadrupole magnetic moments^{4,12,21}. Data is presented as the magnitude of the torque or its field derivative.

Field-angle-resolved electrical resistivity measurements

Additional field-angle-resolved electrical resistivity measurements were carried out with the sample mounted flat on an Attocube piezo rotator, allowing the applied magnetic field direction to be rotated within the NbSe₂ basal plane. Electrical contacts were established using silver-loaded paint. Measurements of the electrical resistance were performed with a Keithley 6221 AC current source in combination with a SR850 digital lock-in amplifier in a constant magnetic field as a function of increasing temperature after field cooling and were repeated for numerous orientations of the in-plane field orientations. The precise parallel sample orientation was ensured with the assistance of an additional goniometer.

Data availability

The data generated in this study have been deposited in the Zenodo database under accession code <https://doi.org/10.5281/zenodo.15627723>.

Code availability

The relevant codes needed to evaluate the findings of this study are available from the corresponding author upon request.

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Author contributions

This work was initiated by R.L. T.T.L. and S.H.C. carried out the DC magnetization measurements. C.-w.C. carried out the magnetic torque experiments with help of C.Y.N. K.T.L. and T.T.L. performed the field angle resolved experiments. A.R.A. and M.A.H. provided the single crystalline sample for the torque measurements. J.P., B.C. and K.P. provided the single crystalline sample for the magnetization measurements. N.F.Q.Y. provided the theoretical simulations and considerations. The manuscript was prepared by R.L. and all authors were involved in discussions and contributed to the manuscript.

Competing interests

The authors declare no competing interests.

Additional information

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